

A NOVEL SORTING METHOD TOPSIS-SORT: AN APPLICATION FOR TEHRAN ENVIRONMENTAL QUALITY EVALUATION

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Introduction

Multiple Criteria Decision Making (MCDM) is all about making choices in the presence of multiple, generally conflicting criteria. Many real-life problems are multi-objective by nature that requires evaluation of more than one criterion. Therefore, MCDM has become an important issue and many researches are devoted to help people make better decision (Montibeller & Franco, 2011; Wang et al., 2015). However, there is no consensus between authors on classification and categorization of MCDM methods. Vincke (1992) suggest the following categories: (1) multiple attribute theory, (2) outranking methods, and (3) interactive methods. Apart from the above, Carlsson & Fuller (1996) classifies these methods into four quite distinct groups: (1) the outranking methods, (2) the value and utility theory approaches, (3) the interactive multiple objective programming approach, and (4) the methods based on group decision and negotiation theory. Comprehensive reviews of MCDM methods can be found in Figueira et al. (2005), Greco et al. (2010), Zavadskas and Turskis (2011), Liou and Tzeng (2012), Zavadskas et al. (2014) and Mardani et al. (2015), their comparative strengths and weaknesses are presented in Belton & Stewart (2002), Zopounidis and Doumpos (2002) and Zardari et al. (2015).

Following Pery (1998), Fernandez et al. (2010), two main categories of problems can be distinguished: preference oriented problems and similarity oriented problems. In preference oriented problems, the decision-maker (DM) wants to select the best alternative or rank all the alternatives from best to worst. In these problems, alternatives are evaluated and compared according to a set of criteria. Usually, higher ranking value means a better performance of the alternative, so the alternative with the highest rank can be considered as best

one, like in ELECTRE, TOPSIS, PROMETHEE and TODIM methods. The similarity oriented problems require sorting of the alternatives into either homogeneous clusters (relative classification) or into pre-defined categories (absolute classification) (Perny, 1998). In case of relative classification, alternatives are divided into clusters based on a set of criteria. According to this approach, most similar alternatives are grouped into a cluster and each alternative's membership in a specific cluster is determined. Therefore, alternatives in the same cluster share many characteristics (i.e. are "similar" to one another), but are very dissimilar to alternatives not belonging to that cluster. In case of absolute classification, alternatives are assigned to some predefined and preference-ordered classes. This group of decision problems is referred to as sorting. Profiles are used to define the classes beforehand as, usually, the bound and limits of each class are determined.

In the outranking methods (OMs), the alternatives are compared pairwise or each alternative is compared to the ideal solution. OMs build a preference relation between alternatives evaluated on several attributes or criteria; in other words, comparison between alternatives is internal. Such methods have nothing to do with the distribution of data, and it is possible there is no one alternative fits into some classes have already defined. However, multiple criteria sorting methods assign alternatives to pre-defined ordered categories taking into account several criteria. Multiple criteria sorting methods differ from standard classification in two main features (Zheng et al., 2014): (1) categories are predefined and ordered, and (2) the sorting model integrates preferences of a decision maker.

The outranking methods are able to provide models that assist for sorting purposes by

employing the outranking relation concept. A representative example of MCDA sorting methods based on the outranking relations approach include methods such as ELECTRE TRI (Mousseau & Slowinski, 1998; Mousseau et al., 2001; Lourenço & Costa, 2004; Brito et al., 2010; Sánchez-Lozano et al., 2014; Bouyssou & Marchant, 2015) and ELECTRE-SORT (Ishizaka & Nemery, 2014), the extensions of the ELECTRE III method. As sorting methods, ELECTRE TRI (also called the non-compensatory sorting model (Bouyssou & Marchant, 2007a; 2007b)) and ELECTRE-SORT are used to assign alternatives to pre-defined categories (Mousseau et al., 2000; Ishizaka & Nemery, 2014). Similar schemes are also employed by other outranking relations sorting methods such as PROMSORT (Araz & Ozkarahan, 2005) and FlowSort (Nemery & Lamboray, 2008; Janssen & Nemery, 2013), which are based on the PROMETHEE method (Preference Ranking Organization Method for Enrichment Evaluation) (see Brans & Vincke, 1985), a well-known multiple criteria outranking method.

In recent years, many MCDM methods have been developed; the existing approaches have been improved and extended. During recent years, many researchers have investigated applicability of MCDM methods and tools to tackle problems that deal with environmental issues. Among numerous MCDM methods developed to solve real-world decision problems, Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) continues to work satisfactorily in diverse application areas (Jiang et al., 2011; Behzadian et al., 2012; Wu, 2015).

The advantage of TOPSIS is its logicity, rationality and computational simplicity (Jiang et al., 2010; Chen et al., 2011). The classical TOPSIS method (see Jia et al., 2012; Ahmadi et al., 2014; Bilbao-Terol et al., 2014; Mulliner et al., 2016) and its extensions, such as interval TOPSIS (see Giove, 2002; Jahanshahloo et al., 2006; Dymova et al., 2013), fuzzy TOPSIS (see Awasthi et al., 2011; Awasthi & Chauhan, 2012; Bao et al., 2012; Ye & Li, 2014; Lee et al., 2014; Kusi-Sarpong et al., 2015; Şengül et al., 2015), interval-valued fuzzy TOPSIS (see Chen & Tsao, 2008; Ashtiani et al., 2009; Chen, 2015; Mokhtarian, 2015; Zhang & Xu, 2015), and grey TOPSIS (see Chen & Tzeng, 2004; Oztaysi, 2014; Siozinyte et al., 2014; Jiang et

al., 2015), have demonstrated their capabilities and potentials in dealing with MCDM problems of various fields.

Sustainability is a complex concept that requires comprehensive analysis (Książek et al., 2015; Xia et al., 2015). Multi criteria decision analysis has been regarded as a suitable set of methods to perform sustainability evaluations (Lazauskaite et al., 2015; Pourahmad et al., 2015). Among numerous MCDM methods employed to solve real world decision problems, Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) continues to be commonly used across different application areas. Jia et al. (2012) utilized both fuzzy AHP and TOPSIS methods for evaluation of the low carbon development (LCD) level of 47 countries (areas). Bilbao-Terol et al. (2014) used TOPSIS for evaluating the countries' sustainability and the sustainability performance of government bond funds. The proposed tool allows investors express their preferences regarding the financial and the ESG (environmental, social and governance) goals, thereby helps them make sustainable and responsible investment decisions. Awasthi et al. (2011) presented fuzzy TOPSIS based approach for evaluation and selection of sustainable transportation systems. Ahmadi et al. (2014) presented an integrated approach that combines the input-output analysis and the TOPSIS method to evaluate sustainability in terms of environmental protection in different sectors of the Iranian economy. Aghajani Mir et al. (2016) proposed an improved version of TOPSIS, which is applied to evaluate the environmental performance of municipal solid waste (MSW) management systems. The proposed model could be used to evaluate various environmental problems associated with solid waste management (e.g. waste reduction, transfer stations for MSW, resource recycling, decommissioning and implementation of waste treatment facilities). Mulliner et al. (2016) presented an empirical application and comparison of different MCDM approaches – the Weighted Sum Model (WSM), the Weighted Product Model (WPM), the revised Analytic Hierarchy Process (AHP), Complex Proportional Assessment (COPRAS) and TOPSIS – for assessing sustainable housing affordability. Therefore, TOPSIS is one of the most commonly used MCDM methods to solve problems associated with different environmental issues.

In this paper, we propose a novel sorting method, TOPSIS-Sort, based on the TOPSIS method. TOPSIS was selected because of its logical concepts and simple computations. Similar to methods discussed previously (e.g. ELECTRE TRI, ELECTRE-SORT and PROMSORT); in the proposed TOPSIS-Sort approach an outranking relation is used for sorting purposes.

The remaining of this paper is organized as follows: In Section 1, we briefly introduce the classical TOPSIS method. Section 2 elaborates the proposed novel sorting method TOPSIS-Sort. An application of the methodology for Tehran environmental quality evaluation is depicted in Section 3. Finally, our conclusions are presented.

1. Overviews of Sorting Theory and TOPSIS

1.1 Problems of Sorting

The sorting problem involves the assignment of a set of alternatives $A = \{a_1, a_2, \dots, a_n\}$ into K predefined ordered classes C_1, C_2, \dots, C_K . Here the order of classes is based on its importance, respectively, C_1 is the best class and C_K is the worst class. The defined classes can be denoted by linguistic variables such as 'surely accepted', 'acceptable', 'rejected', etc. (Norese & Viale, 2002)

A set of reference points is used for sorting, and the alternatives are compared to these reference points. This set of reference points includes a value of reference profiles which specify the theoretical limits between the classes, such as in ELECTRE TRI (Roy & Bouyssou, 1993), or multi-criteria models of a valid (ideal) and a critical (anti-ideal) project, such as in n-TOMIC (Massaglia & Ostanello, 1991).

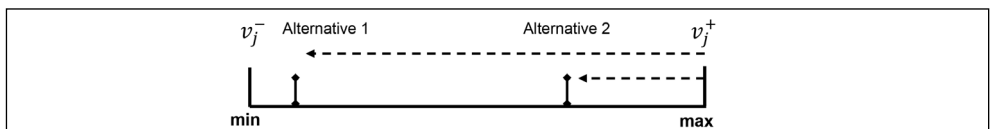
It is worth noting that sorting problems usually refer to absolute evaluation, i.e., the assignment of an alternative does not depend on the remaining ones (Figueira et al., 2005; Bouyssou & Marchant, 2015). In this case, each alternative is assigned to a class on the base of a predefined rule. On the contrary,

both choice and ranking problems are based on relative judgments, involving pairwise comparison between the alternatives (Douplos & Zopounidis, 2002). Consequently, the evaluation result depends on the considered set of alternatives, i.e., each alternative is compared to the others to determine a preference relation.

1.2 TOPSIS; a Brief Reminder

Technique for order preference by similarity to ideal solution (TOPSIS) is one of the most widely used classical MCDM methods, was first developed by Hwang and Yoon (1981). A set of criteria g_1, g_2, \dots, g_m is used to rank the alternatives a_1, a_2, \dots, a_n . Two reference points are determined as ideal solution v_j^+ and anti-ideal solution v_j^- on each criterion. The ideal solution v_j^+ represents the best value for the j th criterion and, conversely, the anti-ideal solution represents the worst value for the j th criterion among all available alternatives. The alternatives with other values lie between these two extremes (v_j^+ and v_j^-). The closer an alternative is to v_j^+ , better performance on the attribute it represents. Contrarily, the farther an alternative is from v_j^+ and the closer to v_j^- , lower value for the attribute it has. As depicted in Fig. 1, Alternative 1 is closer to the negative ideal solution, but farther from the positive ideal solution, whereas Alternative 2 is closer to the positive ideal solution but farther from the negative ideal solution. Thus, Alternative 2 is better choice than Alternative 1 according to the j th criterion. The positive ideal solution (A^+) is composed of all best values attainable of criteria, and the negative ideal solution (A^-) consists of all the worst values attainable of criteria. Finally, all alternatives are ranked according to their distances from the ideal and the negative ideal solution, i.e., the best alternative has simultaneously the shortest distance from the ideal solution and the farthest distance from the negative ideal solution.

Fig. 1: Distance of alternatives from the positive ideal and negative ideal solutions



Source: own

The TOPSIS method consists of the following steps (Vahdani et al., 2011; Dymova et al., 2013):

1. Normalize the decision matrix $X = (x_{ij})_{n \times m}$ using the equation below.

$$r_{ij} = \frac{x_{ij}}{\sqrt{\sum_{i=1}^n x_{ij}^2}}, \quad i = 1, \dots, n; j = 1, \dots, m. \quad (1)$$

2. Calculate the weighted normalized decision matrix $V = (v_{ij})_{n \times m}$.

$$v_{ij} = w_j r_{ij}, \quad i = 1, \dots, n; j = 1, \dots, m, \quad (2)$$

where w_j is the relative weight of the j th criterion, and $\sum_{j=1}^m w_j = 1$.

3. Determine the positive ideal and negative ideal solutions.

$$A^+ = \{v_1^+, \dots, v_m^+\} = \{\max_j v_{ij} | j \in J, \min_j v_{ij} | j \in J'\}, \quad (3)$$

$$A^- = \{v_1^-, \dots, v_m^-\} = \{\min_j v_{ij} | j \in J, \max_j v_{ij} | j \in J'\},$$

where J and J' are the set of benefit criteria and cost criteria, respectively.

4. Calculate the Euclidean distances of each alternative from the positive ideal solution and the negative ideal solution, respectively.

$$D_i^+ = \sqrt{\sum_{j=1}^m (v_{ij} - v_j^+)^2}, \quad i = 1, \dots, n, \quad (4)$$

$$D_i^- = \sqrt{\sum_{j=1}^m (v_{ij} - v_j^-)^2}, \quad i = 1, \dots, n. \quad (5)$$

5. Calculate the relative closeness of each alternative to the ideal solution. The relative closeness of the alternative A_i with respect to A^+ is defined as.

$$c_l = \frac{D_i^-}{D_i^+ + D_i^-}, \quad i = 1, \dots, n. \quad (6)$$

6. Rank the alternatives according to the relative closeness to the ideal solution: the bigger is the c_l , the better is the alternative A_i . The best alternative is the one with the highest relative closeness to the ideal solution.

2. TOPSIS-Sort Method

The TOPSIS-Sort method, proposed by this paper, pertains to the extension of TOPSIS in order to sort the alternatives. The sorting of the alternatives requires their comparison to the reference profiles that distinguish the classes. For each class k , two reference profiles, the upper limit profile \overline{p}^k and the lower limit profile \underline{p}^k , are specified. Upper limit is higher value than the lower limit, i.e., the upper limit of the profile of the first class is greater than the lower limit of the first class $\overline{p}^1 > \underline{p}^1$, and the lower limit of the last class equals the values which are less than the upper limit of the last class $\underline{p}^k < \overline{p}^k$. In other words, all the data values greater than the lower limit of the first class are assigned to the first class, and all the data values less than the upper limit of the last class are properly placed to the last class.

There are two ways to use profiles in the proposed model. The first way is to define the threshold values for each profile based on the decision matrix X . Therefore, 'good' and 'bad' values are assigned to each attribute, and then the position of the attribute values of each alternative in the same interval is determined. The second way is to define the profiles based on the normalized matrix ξ which is calculated using Eq. (7), and then the data can be arranged in the interval $[0, 1]$. Then, some certain intervals are defined for the profiles, for example, very good class $C^1 = \{p^1 = 0.9, p^1 = 1\}$, good class $C^2 = \{p^2 = 0.7, p^2 = 0.9\}$, etc.

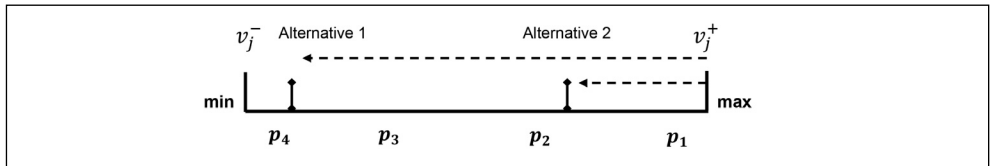
The decision maker's preferences are a significant determinant in solving MCDM problem and should be integrated into the decision model. Each criterion has its own domain of possible values. Taking into account this and DM's preferences with respect to the criteria, the profile values are determined for each class. The criteria can be classified as either benefits or costs. As for the benefit criteria, the values of the profiles of the higher classes are greater, but they decrease towards the lower classes as their appropriateness decreases. In the cost criteria, the values of higher classes are smaller, but they increase towards the lower classes, because the less costly alternative is the most appropriate one. This technique is very useful when there are some evaluation standards.

The TOPSIS method is based on determination of the distance of each alternative from the positive and negative ideal solutions

according to the decision criteria. The profiles are defined as references in the decision matrix, and the distance of the profiles is measured from the positive and negative ideal solutions similar to alternatives (i.e. $cl_{p^k}^+$ and $cl_{p^k}^-$). These two values represent the relative closeness

of the upper limit of the class K to the ideal solution as well as the relative closeness of the lower limit of the class K to the ideal solution. The values of $cl_{p^k}^+$, which lie within the interval $cl_{p^k}^-$ and $cl_{p^k}^+$ fit into the class K (see Fig. 2).

Fig. 2: Distance of alternatives from the positive ideal and negative ideal solutions and position of profiles



Source: own

2.1 TOPSIS-Sort Procedure

The TOPSIS-sort technique for sorting of multiple criteria alternatives includes the following steps:

1. Establish the decision matrix $X = (x_{ij})_{n \times m}$.
2. Determine a set of profiles $P = \{(\overline{p^1}, \underline{p^1}), \dots, (\overline{p^k}, \underline{p^k})\}$, where $\overline{p^k}$ is the upper limit of the class K and $\underline{p^k}$ is the lower limit of the class K .
3. Add the profiles to the decision matrix $\xi = \{X, P\}$.
4. Normalize the decision matrix ξ using the equation below.

$$r_{ij} = \left\{ \frac{\xi_{ij}}{\max} \mid J, 1 - \frac{\xi_{ij}}{\max} \mid J' \right\}, \quad (7)$$

where J and J' denote the sets of benefit criteria and cost criteria, respectively.

5. Execute Steps 1 to 5 of the TOPSIS method.
6. Calculate the values of cl_i for the decision matrix ξ .
7. Determine the values of $cl_{p^k}^+$ and $cl_{p^k}^-$ for the profiles of each $\overline{p^k}$, $\underline{p^k}$ where $cl_{p^k}^+$ refers to the deviation of the upper limit profile of the class K from the ideal solution, and $cl_{p^k}^-$ is the deviation of the lower limit profile of the class K from the ideal solution.

8. Compare the values $cl_{p^k}^+$ with the values $cl_{p^k}^-$ in the profiles using the equation below.

$$a_i^k \in K^k \mid \underline{cl}_{p^k}^+ < cl_j < \overline{cl}_{p^k}^-, \quad (8)$$

$$\forall i = 1, \dots, n, k = 1, \dots, K$$

9. The alternatives whose cl_j values are greater than $\underline{cl}_{p^k}^+$ and less than $\overline{cl}_{p^k}^-$ are assigned to the class K . At this stage the alternatives are sorted and assigned to the classes that are already defined.

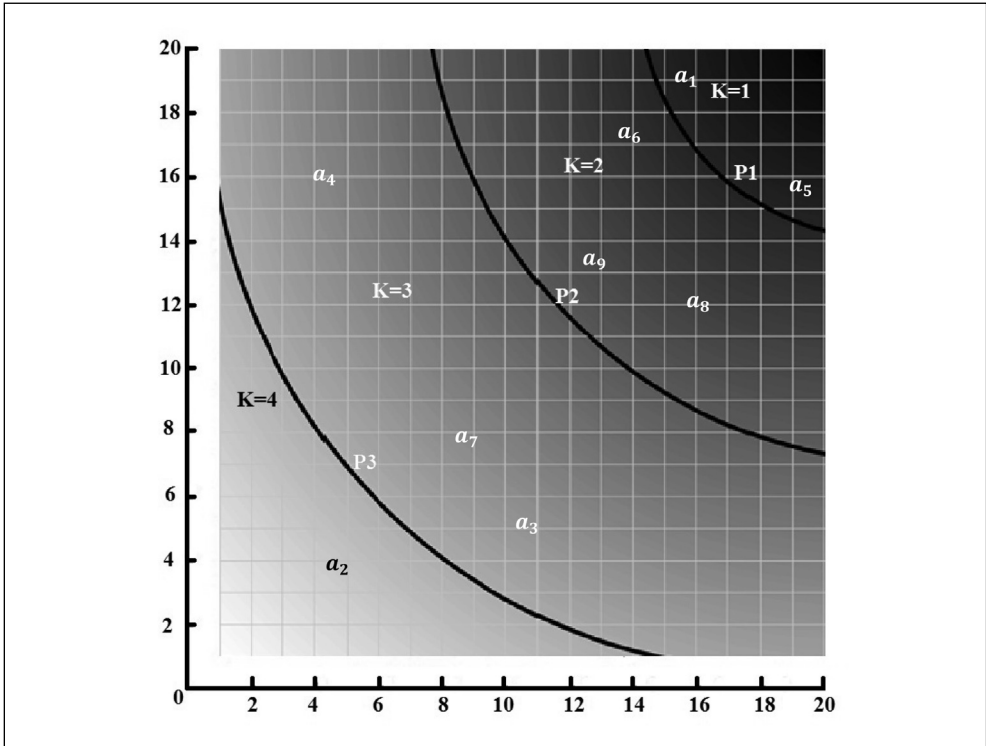
For example, Fig. 3 shows the positive and negative ideal solutions as well as the position of a few assumed alternatives. The curved lines denote a position of the profiles. P1 is the upper limit of Class 1, and all the values that lie within the interval higher than P1 fit into Class 1. P2 is the lower limit and P1 is the upper limit of Class 2, and all the values that lie within this interval belong to Class 2. Alternatives 5 and 1 belong to Class 1, Alternatives 6, 8 and 9 belong to Class 2, Alternatives 4, 7 and 3 belong to Class 3, and Alternative 2 fits into Class 4.

3. An Empirical Case of Tehran

3.1 Classification of Environmental Quality Management

Tehran is the capital city of Iran; it is located in the northern part of the country. Tehran is located on the southern slopes of the Alborz Mountains. With an estimated population of

Fig. 3: Position of profiles and alternatives in the attribute space



Source: own

8.4 million, it is also Iran's largest urban area and city, the largest city in Western Asia, one of the largest in Southern Asia, and the 19th largest city globally. The daily inflow of people, commuting in and out of Tehran, increases the daytime population of the city up to more than 15 million.

Tehran is divided into 22 districts that show remarkable disparities from social, economic, cultural and political points of view. Tehran performs many of national and international functions as a capital city. The ministries, government institutions and other institutions, private companies and branch offices of foreign companies are located in the city. Tehran is the most important transportation hub in Iran in air, rail and road transportation. Almost half of the country's industrial activity is concentrated in Tehran, and it is a significant economic driver across the whole country. However, this has

significant negative impacts on the environment.

The Tehran Metropolis shelters about a quarter of the urban population of Iran, which in itself has led to expansion and escalation of pressures on the environment (Research & Planning Center of Tehran, 2012). Tehran's air pollution is made even worse by the city's geographic position. The city is semi-enclosed in three directions by high altitude mountains, blocking air movements. Therefore, Tehran is facing with numerous environmental problems and issues, such as air pollution mitigation and management, waste management, water and wastewater management, urban safety and greening.

An analysis and assessment of the environmental conditions in Tehran helps to identify the districts with the poor environmental quality. Priority should be given to these areas to maintain and improve the quality

of environment. Tehran's districts can be classified into five classes according to their environmental conditions: high suitable, suitable, moderately suitable, low suitable and very low suitable. The annual report of Tehran municipality was used to define the criteria in order to assess the quality of environment. Five criteria were chosen for evaluation of the urban districts of Tehran. The thresholds of each class were identified using data from the detailed plan of Tehran, Tehran comprehensive plan of greenery, Tehran comprehensive plan of environment and Tehran comprehensive plan of water and wastewater and the specialists' opinion.

Air Pollution

Air pollution is one of the most challenging problems in Tehran. In December 2015, Teheran authorities have decided to close all schools and kindergartens in the capital for two days because of dangerous environmental situation caused by high air pollution. Iran has twice closed schools and government offices because of air pollution, most recently in 2010. According to the office in charge of monitoring air quality, the air in Tehran was pure for only 219 days during the past 16 years (24.com, 2015). Based on AQI (Air Quality Index), during a 10-year period (1983–1993) Tehran experienced 1 dangerous day, 7 very unhealthy days, 67 unhealthy days, 926 unhealthy days for vulnerable people, and 2,481 healthy days out of 3,654 days (<http://air.tehran.ir>). Air pollution was unequally distributed within the city: the pollution was higher in the central areas where the activities were concentrated than in the surroundings.

The national government and local authorities endeavour to develop an efficient air quality management system in Tehran. In order to improve, control and manage the air pollution in Tehran, eleven monitoring stations provide real-time information on air quality and identify the polluted districts. These results can be used by public and involved organizations responsible for the control of air quality.

Urban Green Space

Development of urban green space and landscapes are one of the effective ways for improving air quality, aesthetics and environment. Urban green spaces are known as the lungs of a city (Singh, 2015). Urban

greenery has a natural ability to filter pollution from the air and provide cooling effects during extreme heat (Tiwary et al., 2009; Zupancic et al., 2015). Urban green space improves the environmental quality of life, promotes public health and provides valuable ecosystem services, urban tourism, active and passive recreations to urban dwellers (de Vries, 2003; ECOTEC, 2008; Abraham et al. 2010). Green assets provide benefits both for people, by enhancing public use opportunities, and for the environment by improving urban ecosystem health.

Although the World Health Organization (2010) suggests a minimum of 9 sq. m of green space per capita, this amount is only suitable if the greenery is accessible, good quality and well-maintained. It should be noted that currently accepted standard in Iran for urban green space in cities is 7–12 sq. m. per capita (Ebrahimzadeh et al., 2013). However, access to green spaces is unequally distributed across different areas of Tehran. These problems are caused by the shortage of water and space for urban greenery development, poor soil quality, etc. Unfortunately, over the past years, the urban sprawl and endless construction projects have denuded the city of its green spaces. At present, the green space per capita in Tehran is about 9.2 sq. m, though this amount differs among the districts. This figure indicates that one of environmental challenges in Tehran is shortage of green space. Due to this, air pollution and other environmental problems are becoming crucial in the city. Thus, this criterion is of great importance for evaluation of the quality of urban environment.

Waste

According to the Tehran Waste Management Organization, every resident of Tehran produces 320 kilograms of solid waste per year. In other words, annually every resident produces an average 6 times more waste than his/her weight. While the average per capita production of solid waste in the world is 250–300 grams per day, Iran daily produces an average 600 grams per person. In northern Tehran, this amount reaches 1,200 grams. In central Tehran, especially District 20, where the commercial facilities are concentrated, the waste production rate reaches its peak. Statistics show that business districts of Tehran produce more waste, and the waste produced

in the northern Tehran is at least 2 times more than the country average and 4 times more than the world average.

Water and Wastewater

Urban water is used to meet commercial, industrial, institutional and residential needs of the city. Water is involved in domestic and productive/irrigation activities. Citizens should be provided with sufficient and safe water to meet their basic needs, i.e., for drinking, cooking, and personal and domestic hygiene. Tehran is located in a semi-arid region with little rainfall and frequent droughts. The mean annual precipitation is only 250 millimeters, most of which falls during winter and spring. Tehran is facing with a water shortage of more than 100 million cubic meters (MCM) per year in drought years. The most important freshwater resources in Tehran are the Karaj, Lar, Latian, Mamloo and Taleghan reservoirs. Tehran supplements surface water with groundwater to mitigate the water shortage, and at least 250 MCM of water is discharged from wells annually in Tehran (Tajrishy et al., 2014).

According to the Tehran Water and Wastewater Company, over 703 MCM of water is supplied to Tehran, and on average 85 MCM per month is extracted and supplied to the city, out of which 71.7 come from surface water and the rest from the groundwater. The total water consumption of the Tehran province was about 980 MCM in 2008. During summer months water consumption and demand for domestic water increases as the summer heat rises in densely populated Tehran.

Expansion of urban population and increased household water consumption and sewerage give rise to greater quantities of municipal wastewater. With emphasis on environmental health issues, there is an increasing awareness of the need to dispose the wastewater safely and beneficially.

Ratio of Incident to Station

According to the Fire Organization, 12,620 fires incidents have occurred in residential, commercial, administrative and industrial properties in Tehran during 2007. The highest number of fires was in District 2, while District 13 experienced the least number of incidents. Population density, old electrical wires and connections, storage of flammable materials in residential places, using substandard electric

and gas appliances, and ignoring safety regulations, these are some of the causes of fire in residential property in Tehran.

3.2 Application of TOPSIS-Sort

Five criteria are used to classify Tehran’s districts on the quality of urban environment: urban green space per capita (g_1), waste and soil pollution management (g_2), quality of environmental management of water and wastewater projects (g_3), air pollution management (g_4), ratio of incidents to station (g_5). These criteria are taken into account in order to identify five classes of districts, also to determine the costs and benefits of each alternative and the weight of the criteria. Therefore, Class 1 is considered as the best and then Classes 2 to 5 are ranked respectively. Taking into account the specialists’ opinion and data from the comprehensive plans of Tehran, the upper limit profile and the upper limit profile for each class was defined. The standards compatible with Tehran have been deployed in defining the profiles, so the profiles are independent from the alternatives and their scores. The profiles are shown in Tab. 2. The weight of all criteria is assumed the same (0.2). The scores of 22 districts of Tehran according to the criteria were collected and entered into the decision matrix (Tab. 2). Then, the matrix and the profile were combined together (Tab. 3). Fig. 4 provides a graphical representation of the position of three districts (1, 6 and 21) according to the defined profiles. At the next step, the decision matrix and the profile were normalized by Eq. (7). The weight normalized matrix is obtained by multiplying the normalized decision matrix with the weights vector. At the next step, the values of the positive and negative ideal solutions were determined for each criterion (Tab. 3).

In the next step, the distance from the positive and negative ideal solutions is calculated using Eqs. (4) and (5) (Tab. 4). According to Eq. (6), the deviation of the alternatives cl_j from the ideal solution is determined and the deviation of profile from the ideal solution (cl_j^{pr} and cl_j^{pr}) is also calculated. Final step, the deviation of profile from the ideal solution is calculated and then the alternatives are assigned to the classes through comparison between cl_j of each alternative and cl_j of profiles. For example, cl_j of District 1 is 0.54753 which is less than Profile 1, so it does not fit into Class 1. This value is greater than Profile 2 (0.51037),

so it belongs to Class 2. The cl_j of Alternative 3 is 49,401 which is less than the lower limit of Class 1, so it does not fit into Class 1. Now it is the turn of Class 2. This value is compared to the lower limit of Class 2. Alternative 3 does not fit into Class 2, because it is less than the lower limit of Class 2. Alternative 3 belongs to Class 3, since it is greater than the lower limit of Class 3 but less than its upper limit. In this way cl_j of all alternatives are compared to the

values of cl_j^k and $\overline{cl_j^k}$ in order to determine their related classes. It should be noted, that none of the alternatives fits into Classes 4 and 5 (see Fig. 5). Thus, all the alternatives are classified; Class 1 turns out to be the best and Class 5 would be the worst. Sorting results of 22 districts of Tehran according to the set of criteria are shown in Tab. 5.

Tab. 1: Specifications of the classification for the quality of Tehran environmental management

	Criteria				
	g_1	g_2	g_3	g_4	g_5
Cost/Benefit	benefit	benefit	benefit	benefit	cost
Weight	0.2	0.2	0.2	0.2	0.2
p_1	25	80	40	80	150
p_2	20	75	30	60	300
p_3	10	70	20	30	400
p_4	0	65	10	20	700

Source: own

Tab. 2: Decision matrix for environmental quality evaluation in districts of Tehran (Part 1)

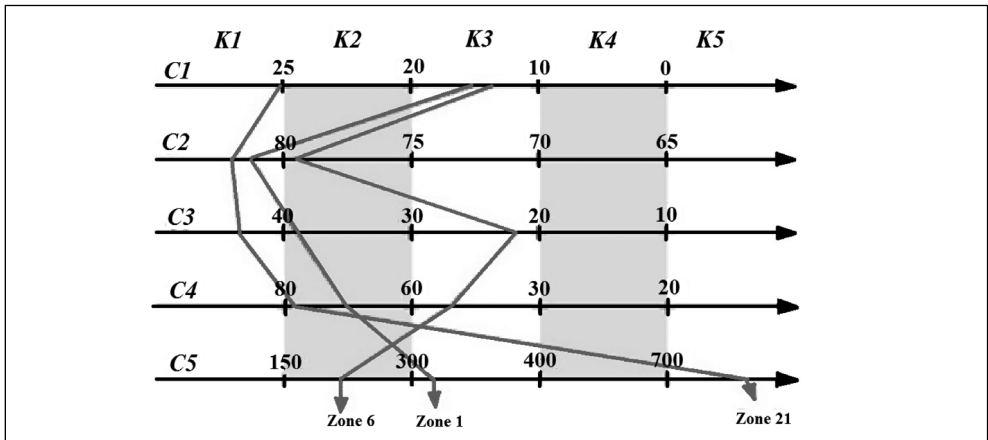
Districts	Criteria				
	g_1	g_2	g_3	g_4	g_5
1	15.50	82.40	40.10	70.66	313.69
2	9.90	90.80	22.00	82.21	130.61
3	15.20	82.30	25.20	65.57	269.37
4	23.40	88.30	60.20	69.28	119.03
5	16.60	76.80	22.70	69.28	116.82
6	12.40	78.60	22.60	50.28	199.55
7	4.00	85.00	27.80	51.40	188.94
8	4.40	78.20	25.60	56.59	126.37
9	5.20	80.20	27.60	86.29	108.82
10	2.30	80.70	24.20	79.88	97.95
11	4.90	77.70	26.30	61.28	122.58
12	5.70	80.90	26.80	70.75	82.75
13	33.40	85.30	28.10	67.68	126.14
14	5.90	82.50	29.80	82.61	149.32
15	14.00	88.50	24.60	90.71	335.24
16	11.40	81.80	26.50	61.04	139.62
17	3.50	78.90	22.40	60.82	99.42

Tab. 2: Decision matrix for environmental quality evaluation in districts of Tehran (Part 2)

Districts	Criteria				
	g_1	g_2	g_3	g_4	g_5
18	12.96	78.40	25.20	67.25	180.18
19	28.00	82.40	25.30	56.89	102.78
20	15.70	82.10	27.70	24.64	193.52
21	25.00	91.30	67.10	79.81	916.67
22	48.00	85.10	49.20	86.71	173.79
p_1	25	80	40	80	150
p_2	20	75	30	60	300
p_3	10	70	20	30	400
p_4	0	65	10	20	700

Source: own

Fig. 4: Profiles and classes of environmental quality evaluation and the position of Tehran Districts 1, 6 and 21



Source: own

Tab. 3: Profiles and normalized weight matrix (Part 1)

Districts & Profiles	Criteria				
	g_1	g_2	g_3	g_4	g_5
1	0.0646	0.1805	0.1195	0.1558	0.0684
2	0.0413	0.1989	0.0656	0.1813	0.0285
3	0.0633	0.1803	0.0751	0.1446	0.0588
4	0.0975	0.1934	0.1794	0.1528	0.0260
5	0.0692	0.1682	0.0677	0.1528	0.0255
6	0.0517	0.1722	0.0674	0.1109	0.0435

Tab. 3: Profiles and normalized weight matrix (Part 2)

Districts & Profiles	Criteria				
	g_1	g_2	g_3	g_4	g_5
7	0.0167	0.1862	0.0829	0.1133	0.0412
8	0.0183	0.1713	0.0763	0.1248	0.0276
9	0.0217	0.1757	0.0823	0.1903	0.0237
10	0.0096	0.1768	0.0721	0.1761	0.0214
11	0.0204	0.1702	0.0784	0.1351	0.0267
12	0.0238	0.1772	0.0799	0.1560	0.0181
13	0.1392	0.1869	0.0838	0.1492	0.0275
14	0.0246	0.1807	0.0888	0.1821	0.0326
15	0.0583	0.1939	0.0733	0.2000	0.0731
16	0.0475	0.1792	0.0790	0.1346	0.0305
17	0.0146	0.1728	0.0668	0.1341	0.0217
18	0.0540	0.1717	0.0751	0.1483	0.0393
19	0.1167	0.1805	0.0754	0.1254	0.0224
20	0.0654	0.1798	0.0826	0.0543	0.0422
21	0.1042	0.2000	0.2000	0.1760	0.2000
22	0.2000	0.1864	0.1466	0.1912	0.0379
Profile 1	0.1042	0.1752	0.1192	0.1764	0.0327
Profile 2	0.0833	0.1643	0.0894	0.1323	0.0655
Profile 3	0.0417	0.1533	0.0596	0.0661	0.0873
Profile 4	0.0000	0.1424	0.0298	0.0441	0.1527
Ideal	0.2000	0.2000	0.2000	0.2000	0.0181
Anti-Ideal	0.0000	0.1424	0.0298	0.0441	0.2000

Source: own

Tab. 4: Distances of alternatives and profiles from the ideal solution (Part 1)

Districts & Profiles	Ideal	Anti-Ideal	CI
1	0.17230	0.20850	0.54753
2	0.20910	0.23320	0.52724
3	0.19850	0.19380	0.49401
4	0.11520	0.27680	0.70612
5	0.19480	0.22170	0.53229
6	0.22130	0.18410	0.45412
7	0.23570	0.18710	0.44253
8	0.23430	0.19890	0.45914
9	0.21540	0.23820	0.52513
10	0.23180	0.22890	0.49685
11	0.22850	0.20460	0.47241
12	0.21900	0.22340	0.50497

Tab. 4: Distances of alternatives and profiles from the ideal solution (Part 2)

Districts & Profiles	Ideal	Anti-Ideal	CI
13	0.14160	0.25510	0.64306
14	0.20980	0.22940	0.52231
15	0.19800	0.21990	0.52620
16	0.20680	0.20730	0.50060
17	0.23920	0.20590	0.46259
18	0.20210	0.20620	0.50502
19	0.16860	0.23510	0.58236
20	0.23260	0.18290	0.44019
21	0.20700	0.24600	0.54305
22	0.05920	0.32170	0.84458
Profile 1	0.13070	0.25570	0.66175
Profile 2	0.18420	0.19200	0.51037
Profile 3	0.26390	0.12620	0.32351
Profile 4	0.33870	0.04730	0.12254

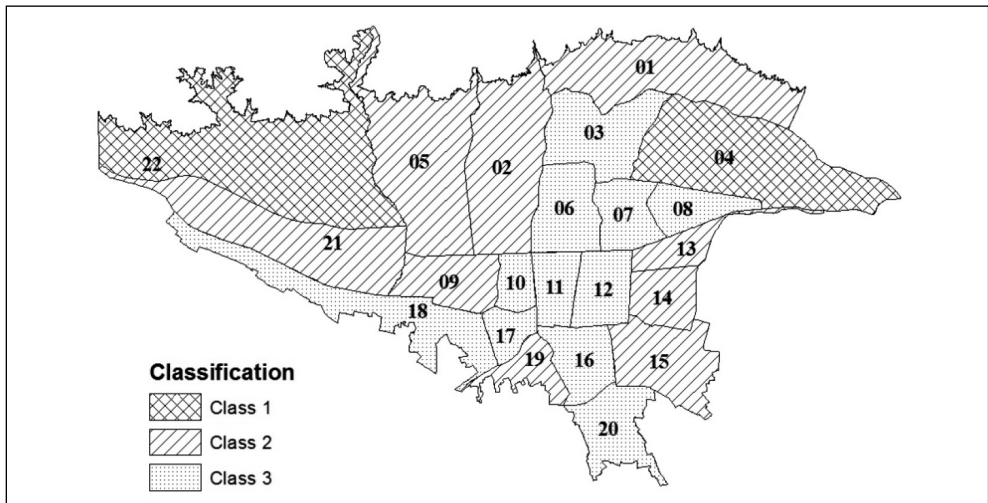
Source: own

Tab. 5: Sorting of the districts of Tehran by the method TOPSIS-Sort

District	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22
Class	2	2	3	1	2	3	3	3	2	3	3	3	2	2	2	3	3	3	2	3	2	1

Source: own

Fig. 5: Classification of Tehran districts by the method TOPSIS-Sort



Source: own

Conclusions

For solution of a MCDM problem, there exist different methods for outranking alternatives, in which the alternatives are compared pairwise or each alternative is compared to the ideal solution. The best and worst values of attributes as reference points are internally defined, and the alternative with the best performance on all attributes is regarded as ideal to which other alternatives are compared. The alternatives can also be compared pairwise against each of the criteria for preference, and a complete ranking of alternatives from the best to the worst one is provided. If reference points are externally defined for comparison, we achieve a set of methods that sort the alternatives into pre-defined categories.

The TOPSIS-Sort method, proposed in this paper, pertains to the extension of the classic TOPSIS method in order to sort the alternatives. In the proposed method, the profile and reference points determine a range from the best to the worst values independently from the data. Application of the proposed approach was demonstrated by classifying 22 districts of Tehran into five classes (but none of the districts fits into Classes 4 and 5), representing areas with different levels of environmental quality. The results obtained by the TOPSIS-Sort give credence to its success, because the results of sorting confirm our and specialists' evaluation of the districts. This research provides appropriate results with respect to the development of sorting models in the form of outranking relations. The model, proposed by this study, is applicable to the other outranking methods such as ELECTRE, PROMETHEE, etc.

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Abstract

A NOVEL SORTING METHOD TOPSIS-SORT: AN APPLICATION FOR TEHRAN ENVIRONMENTAL QUALITY EVALUATION**Hassanali Faraji Sabokbar, Ali Hosseini, Audrius Banaitis, Nerija Banaitiene**

Many real-life problems are multi-objective by nature that requires evaluation of more than one criterion, therefore MCDM has become an important issue. In recent years, many MCDM methods have been developed; the existing approaches have been improved and extended. Multi criteria decision analysis has been regarded as a suitable set of methods to perform sustainability evaluations. Among numerous MCDM methods developed to solve real-life decision problems, Technique for Order Preference by Similarity to Ideal Solution (TOPSIS) continues to work satisfactorily in diverse application areas. In this paper, a novel sorting method (TOPSIS-Sort) based on the classic TOPSIS method is presented. In the TOPSIS-Sort approach an outranking relation is used for sorting purposes. The proposed approach uses characteristic profiles for defining the classes and outranking relation as the preference model. Application of the proposed approach is demonstrated by classifying 22 districts of Tehran into five classes (but none of the districts fits into Classes 4 and 5), representing areas with different levels of environmental quality. An analysis and assessment of the environmental conditions in Tehran helps to identify the districts with the poor environmental quality. Priority should be given to these areas to maintain and improve the quality of environment. The results obtained by the TOPSIS-Sort give credence to its success, because the results of sorting confirm our and specialists' evaluation of the districts. This research provides appropriate results with respect to the development of sorting models in the form of outranking relations. The model, proposed by this study, is applicable to the other outranking methods such as ELECTRE, PROMETHEE, etc.

Key Words: TOPSIS-Sort, multiple criteria decision making (MCDM), outranking, sorting.

JEL Classification: C02, C44, C61, C88, O18, Q56.

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